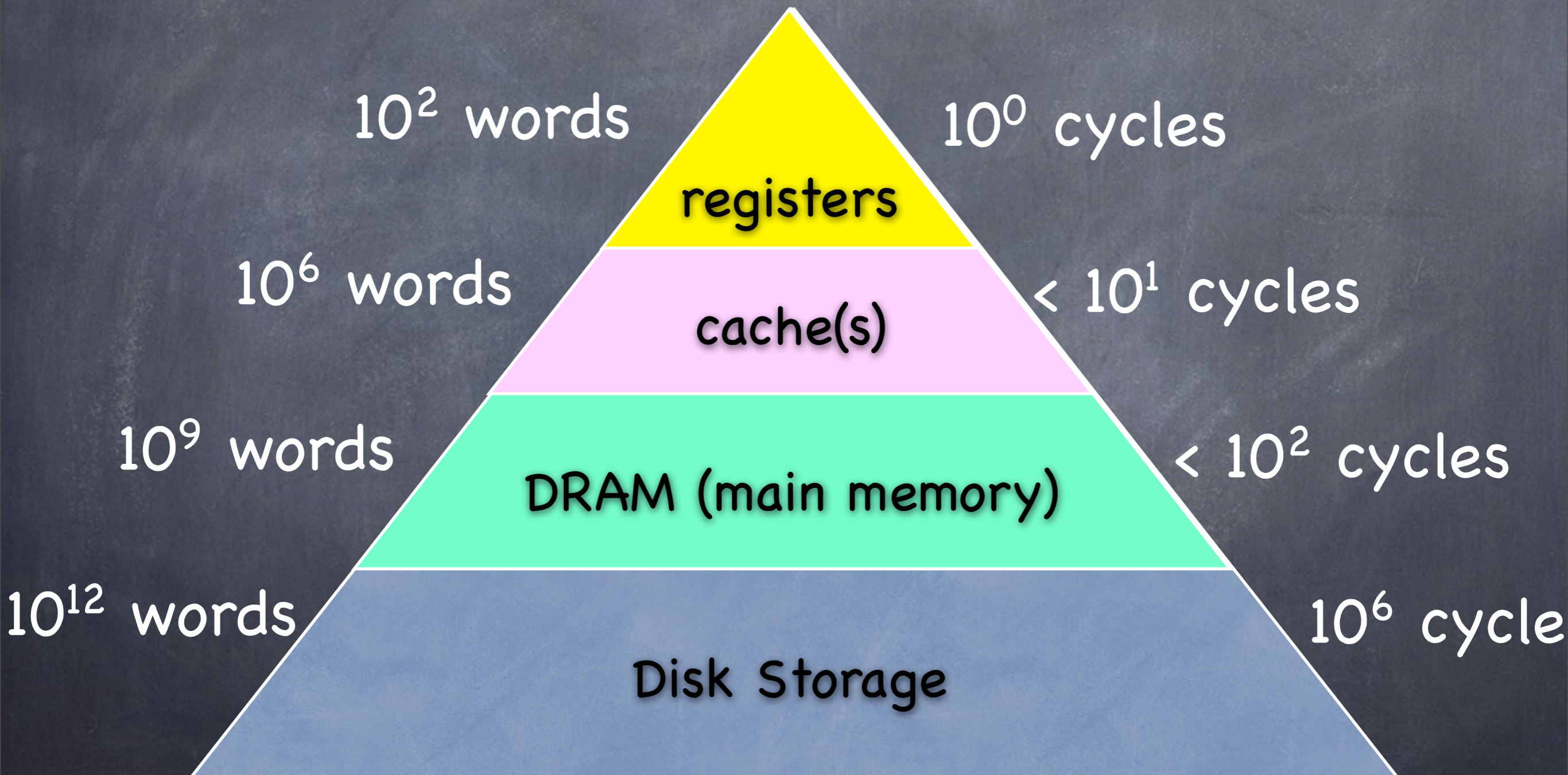


Announcements

TA Application Time - Due by Monday

Cash, Cache, or Cachet?



Units and Measures

	inch	foot	yard	fathom
Length in inches	1	12	36	72

inches away	in inches	in feet	in yards	in fathoms
0	0	0	0	0
12	4	1	?	?
72	72	6	2	1
360	360	30	10	5

Memory Units and Addresses

	byte	word	cache block	page
Size in bytes	1	4	16	1024

byte number	byte address	word address	cache block number	page number
0	0	0	0	0
4	4	1	?	?
16	16	4	1	?
1024	1024	256	63	1
8196	8196	2048	512	8

Memory Units and Addresses

	byte	word	cache block	page
Size in bytes	1	4	16	1024

byte number	byte address	word address	cache block number	page number
0	0	0	0	0
4	4	1	0	0
16	16	4	1	0
1024	1024	256	63	1
8196	8196	2048	512	8

Memory Units and Addresses

	byte	word	cache block	page
Size in bytes	1	4	4	4096

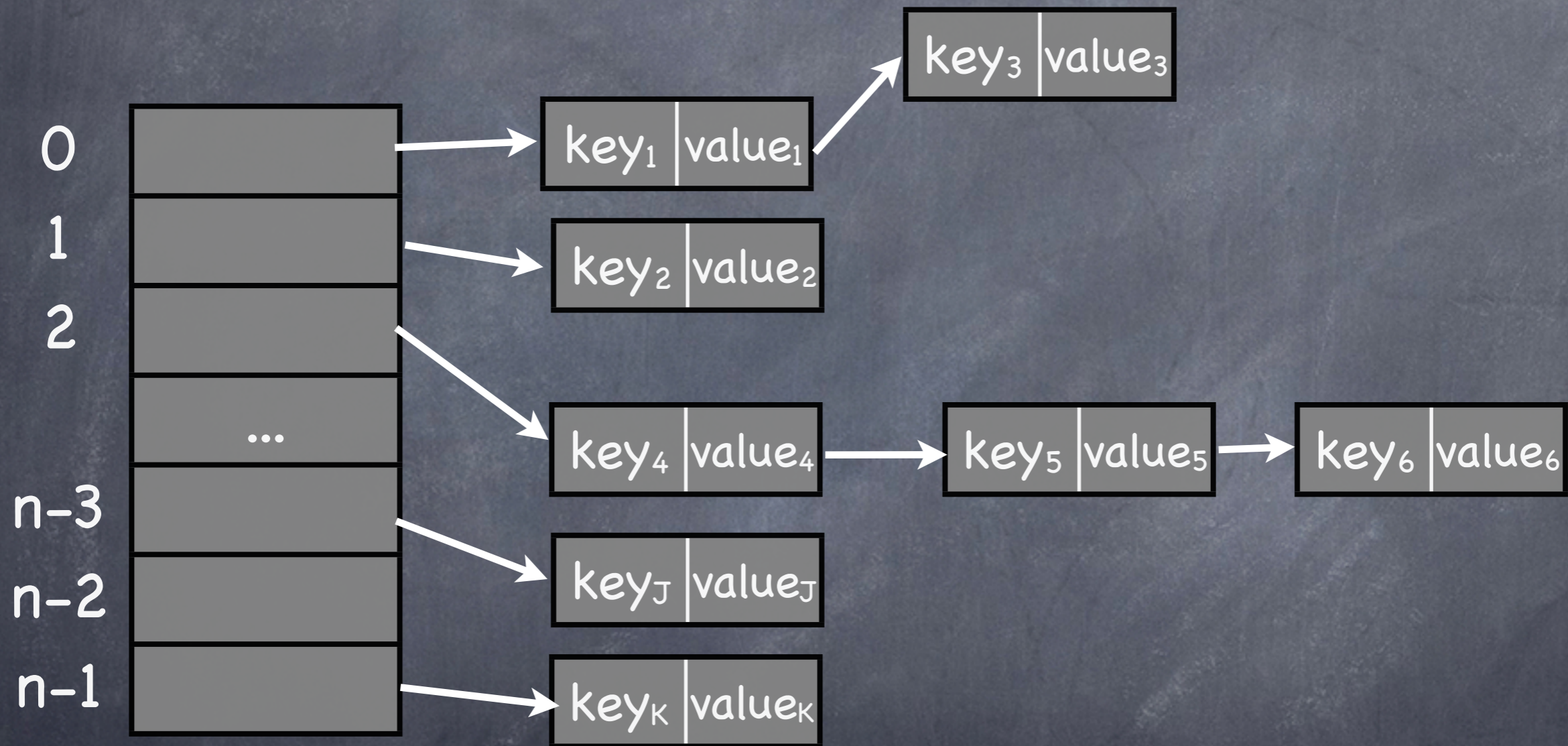
byte number	byte address	word address	cache block number	page number
0	0	0	0	0
4	4	1	1	0
16	16	4	4	0
1024	1024	256	256	0
8196	8196	2048	2048	2

Memory Units and Addresses

	byte	word	cache block	page
Size in bytes	1	100 = 4	10000 = 16	10000000000 = 1024

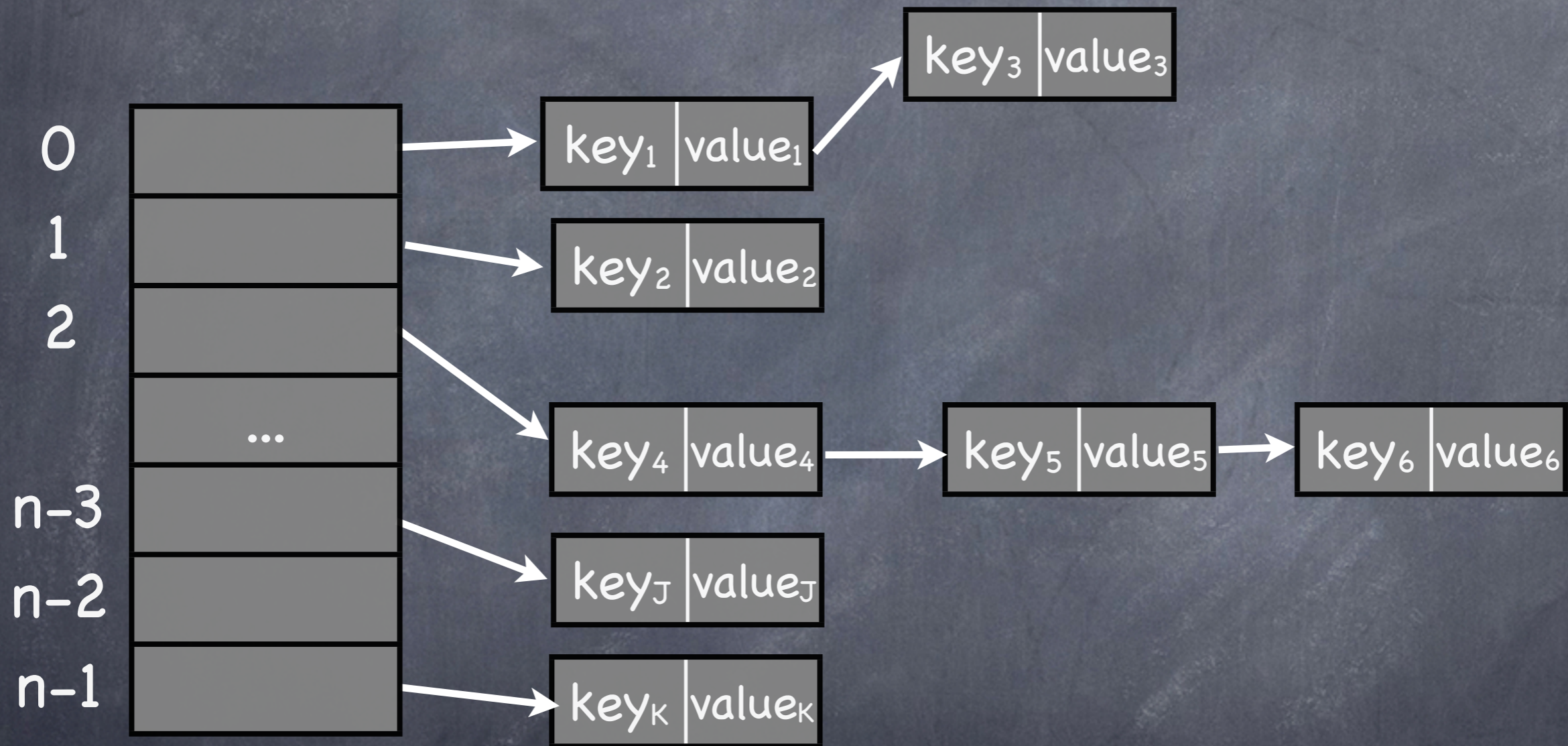
byte number	byte address	word address	cache block number	page number
00000000100	00000000100	00000001	000000	0
0000010000	0000010000	00000100	000001	0
1000000000	1000000000	10000000	100000	1

Hash vs. Cache



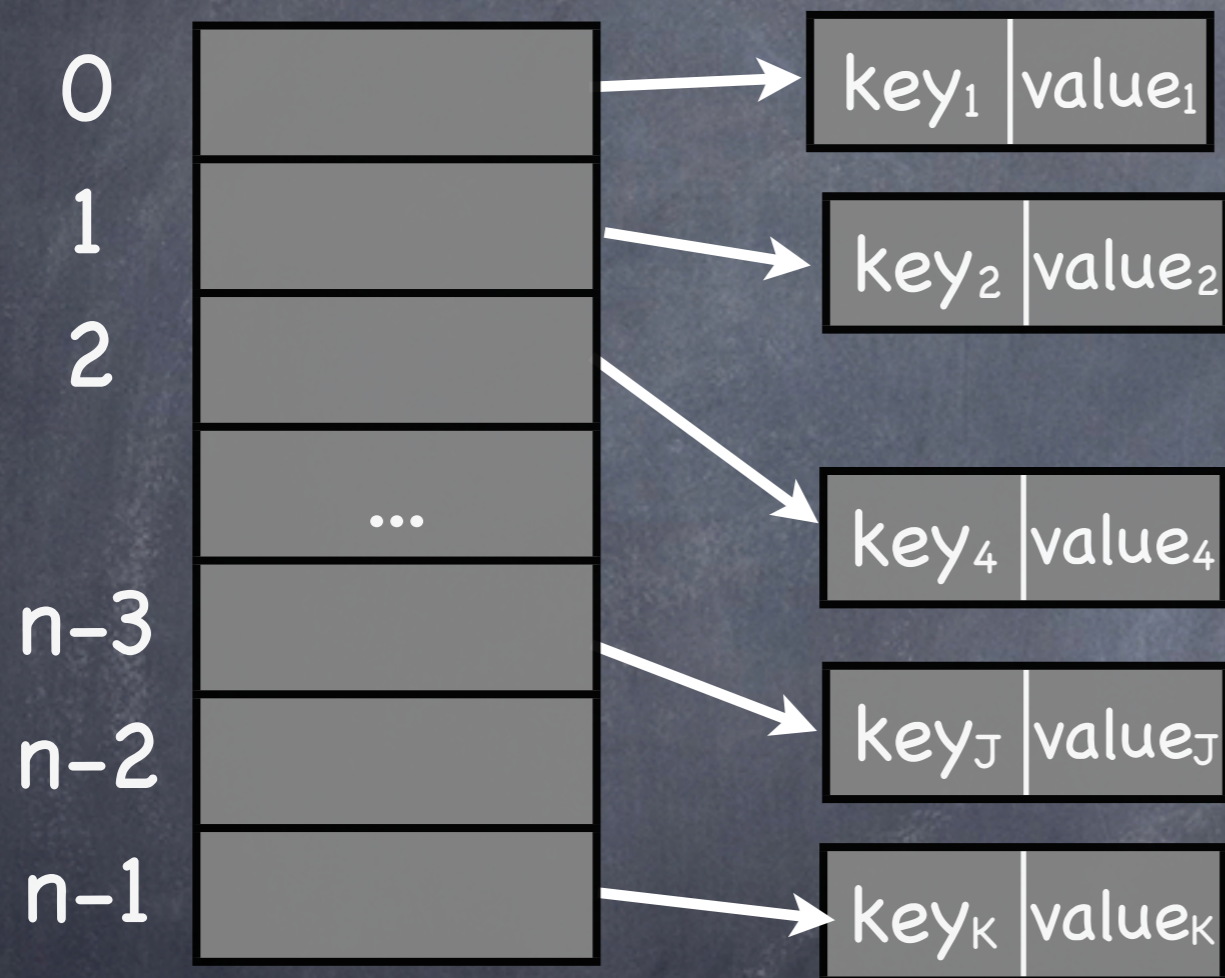
- Hash function maps keys to "random" bins
- Lookup within bins by linked list traversal

Forgetful Hash vs. Cache



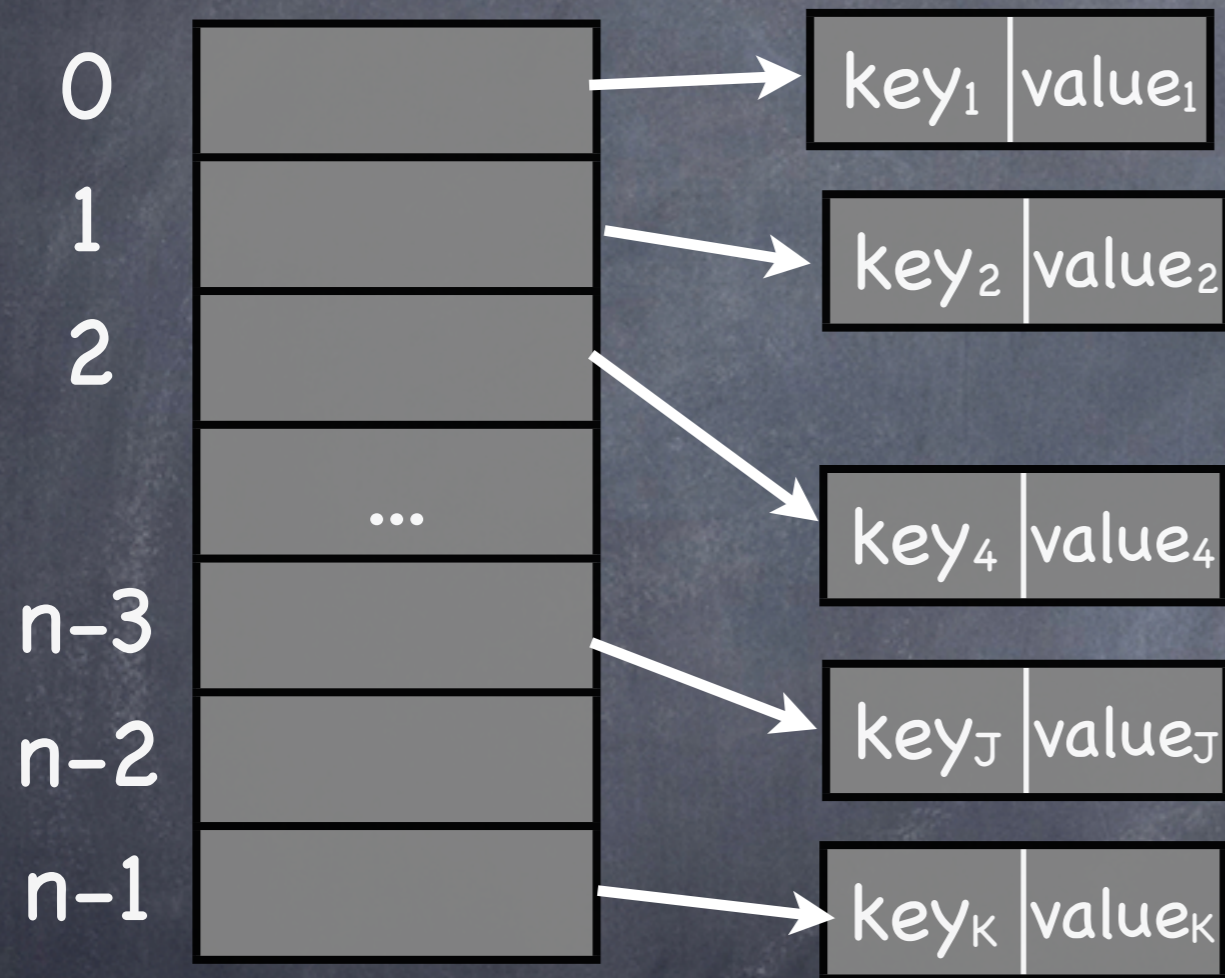
- Only keep first item in each hash bin list

Forgetful Hash vs. Cache



- Only keep first item in each hash bin list

Forgetful Hash vs. Cache



• No need for linked lists of size one!


Forgetful Hash vs. Cache

0	key ₁ value ₁
1	key ₂ value ₂
2	key ₄ value ₄
	...
n-3	key _J value _J
n-2	
n-1	key _K value _K

- No need for linked lists of size one!

Forgetful Hash vs. Cache

$\text{bin} = \text{hash}(\text{key}_{\text{search}})$



The diagram shows an arrow pointing from the expression $\text{bin} = \text{hash}(\text{key}_{\text{search}})$ to the index '2' in the table below.

0	key ₁	value ₁
1	key ₂	value ₂
2	key ₄	value ₄

n-3	key _J	value _J
n-2		
n-1	key _K	value _K

- To find a particular key, first hash the key

Forgetful Hash vs. Cache

```
bin = hash( keysearch )
```

```
if ( keybin == keysearch ) {  
    hit = true;  
    value = valuebin;  
} else {  
    hit = false;  
}
```

0	key ₁	value ₁
1	key ₂	value ₂
2	key ₄	value ₄

n-3	key _J	value _J
n-2		
n-1	key _K	value _K

• Check key in bin to determine whe

Forgetful Hash vs. Cache

$\text{bin} = \text{hash}(\text{key}_{\text{search}})$



$\text{hash}(v) = v \% n$

0	key ₁	value ₁
1	key ₂	value ₂
2	key ₄	value ₄

n-3	key _J	value _J
n-2		
n-1	key _K	value _K

👁️ Everyone's favorite hash function?

Forgetful Hash vs. Cache

$\text{bin} = \text{hash}(\text{key}_{\text{search}})$

0

key ₁	value ₁
------------------	--------------------

1

key ₂	value ₂
------------------	--------------------

2

key ₄	value ₄
------------------	--------------------

...

...

n-3

key _J	value _J
------------------	--------------------

n-2

n-1

key _K	value _K
------------------	--------------------

$$\text{hash}(v) = v \% 2^n$$

👁️ Everyone's favorite hash function!

Forgetful Hash vs. Cache

$\text{bin} = \text{hash}(\text{key}_{\text{search}})$

0

key ₁	value ₁
------------------	--------------------

1

key ₂	value ₂
------------------	--------------------

2

key ₄	value ₄
------------------	--------------------

...

...

n-3

key _J	value _J
------------------	--------------------

n-2

n-1

key _K	value _K
------------------	--------------------

$\text{hash}(v) = v \% 2^n$
= last n bits of v

👁️ Everyone's favorite hash function!

Cache

bin = last n bits of
cache block number

$$\text{hash}(v) = v \% 2^n$$

= last n bits of v

0	cache blk num ₁	blk contents ₁
1	cache blk num ₂	blk contents ₂
2	cache blk num ₄	blk contents ₄

n-3	cache blk num _J	blk contents _J
n-2		
n-1	cache blk num _K	blk contents _K

- In cache, key = block number, value = contents

Saving a few bits

$$\text{bin} = \text{blk num} \% 2^n$$



0	cache blk num ₁ / 2 ⁿ	blk contents ₁
1	cache blk num ₂ / 2 ⁿ	blk contents ₂
2	cache blk num ₄ / 2 ⁿ	blk contents ₄

n-3	cache blk num _J / 2 ⁿ	blk contents _J
n-2		
n-1	cache blk num _K / 2 ⁿ	blk contents _K

- bin number = last n bits of blk num

Valid bits

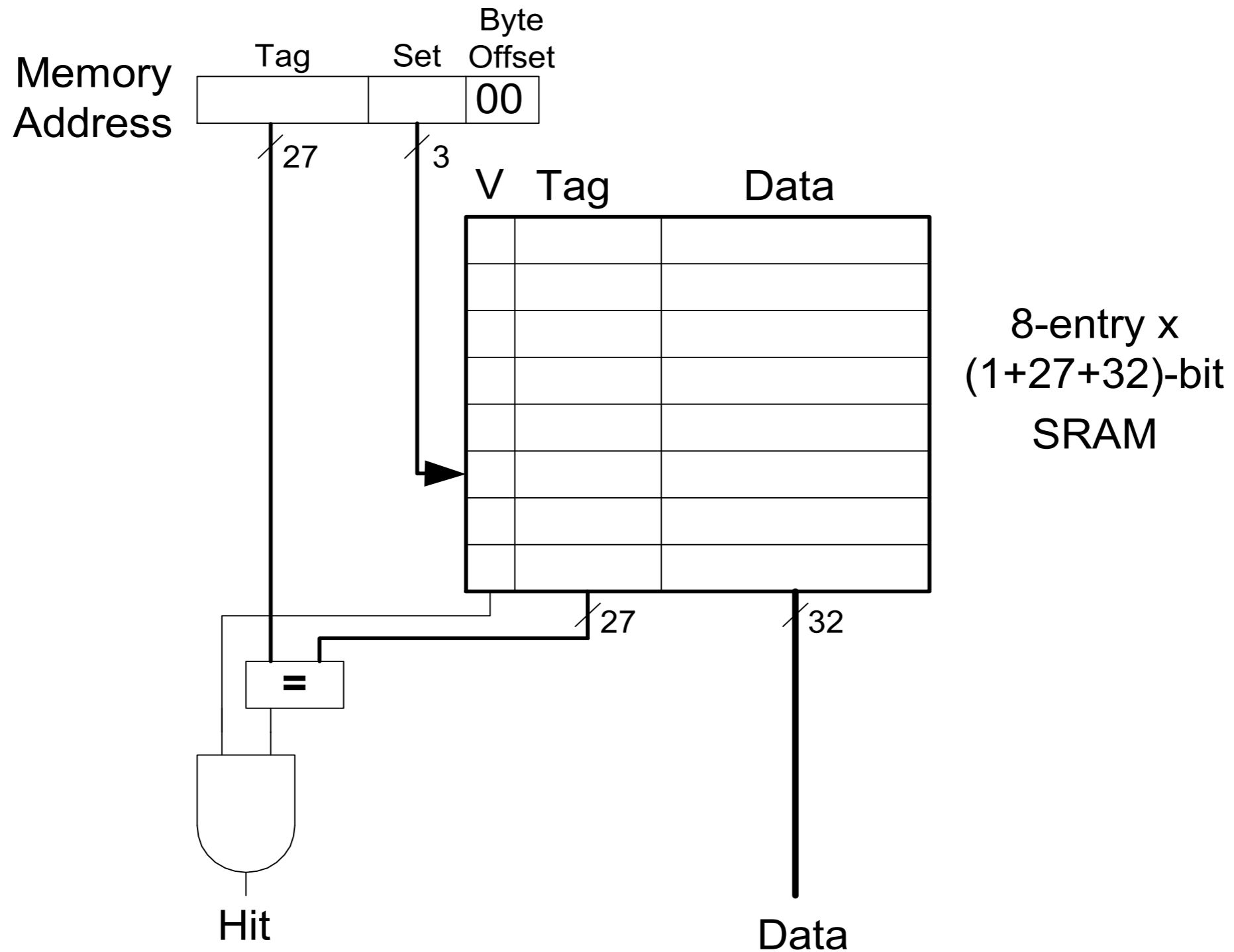
$$\text{bin} = \text{blk num} \% 2^n$$

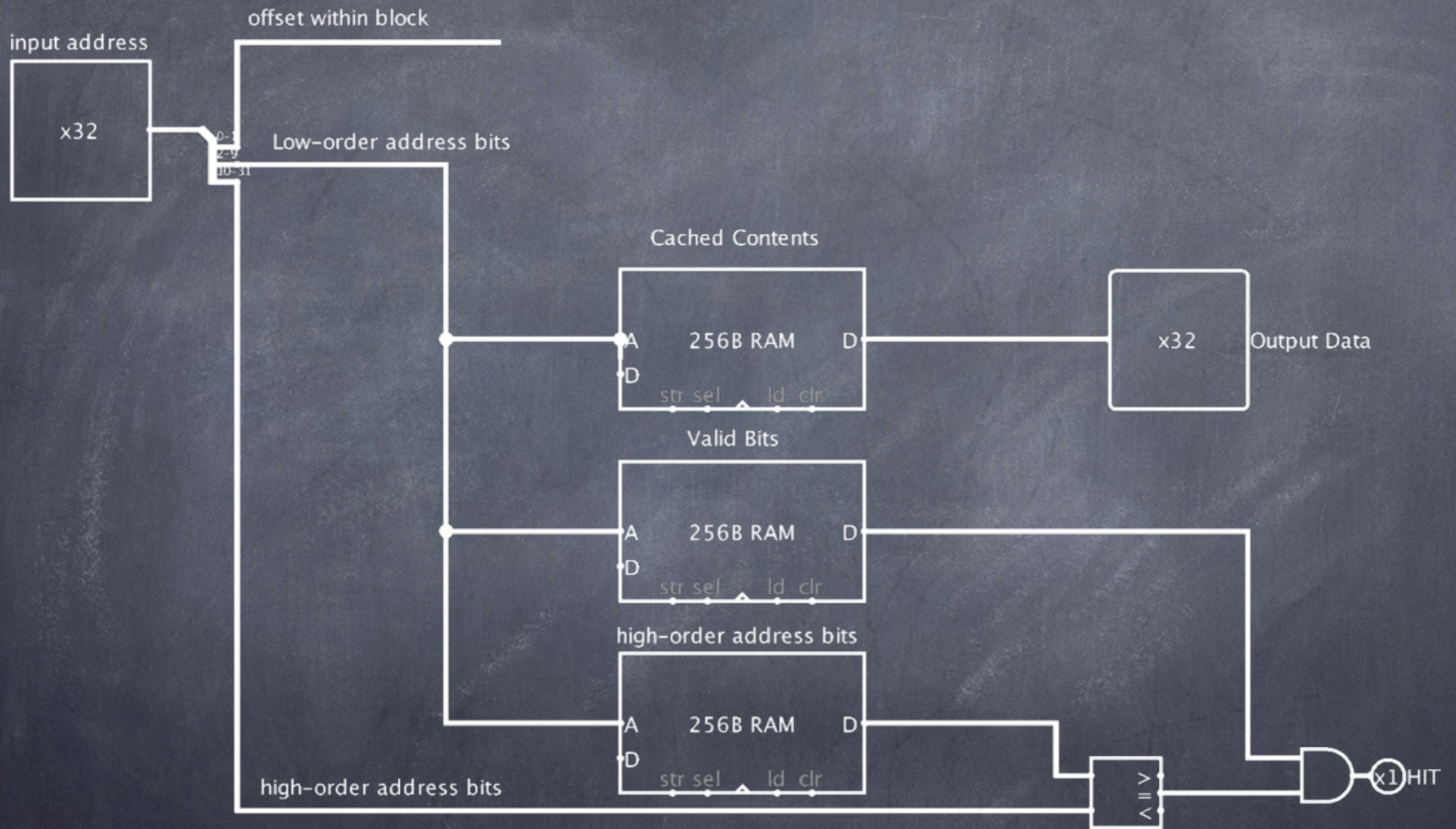


0	x	cache blk num ₁ / 2 ⁿ	blk contents ₁
1	x	cache blk num ₂ / 2 ⁿ	blk contents ₂
2	x	cache blk num ₄ / 2 ⁿ	blk contents ₄
	-
n-3	x	cache blk num _J / 2 ⁿ	blk contents _J
n-2	-		
n-1	x	cache blk num _K / 2 ⁿ	blk contents _K

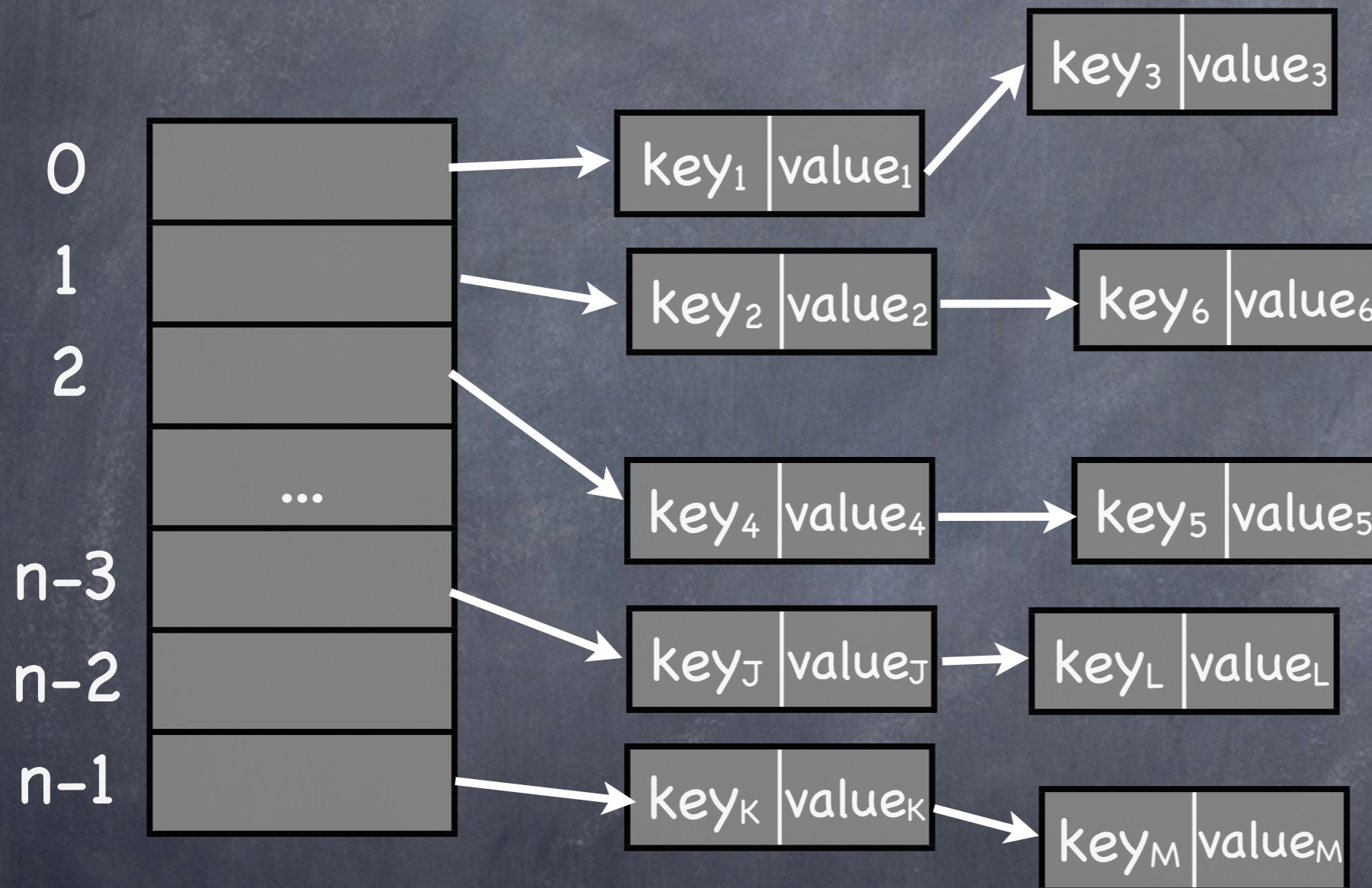
- Valid bit marks empty cache entries

Direct Mapped Cache Hardware



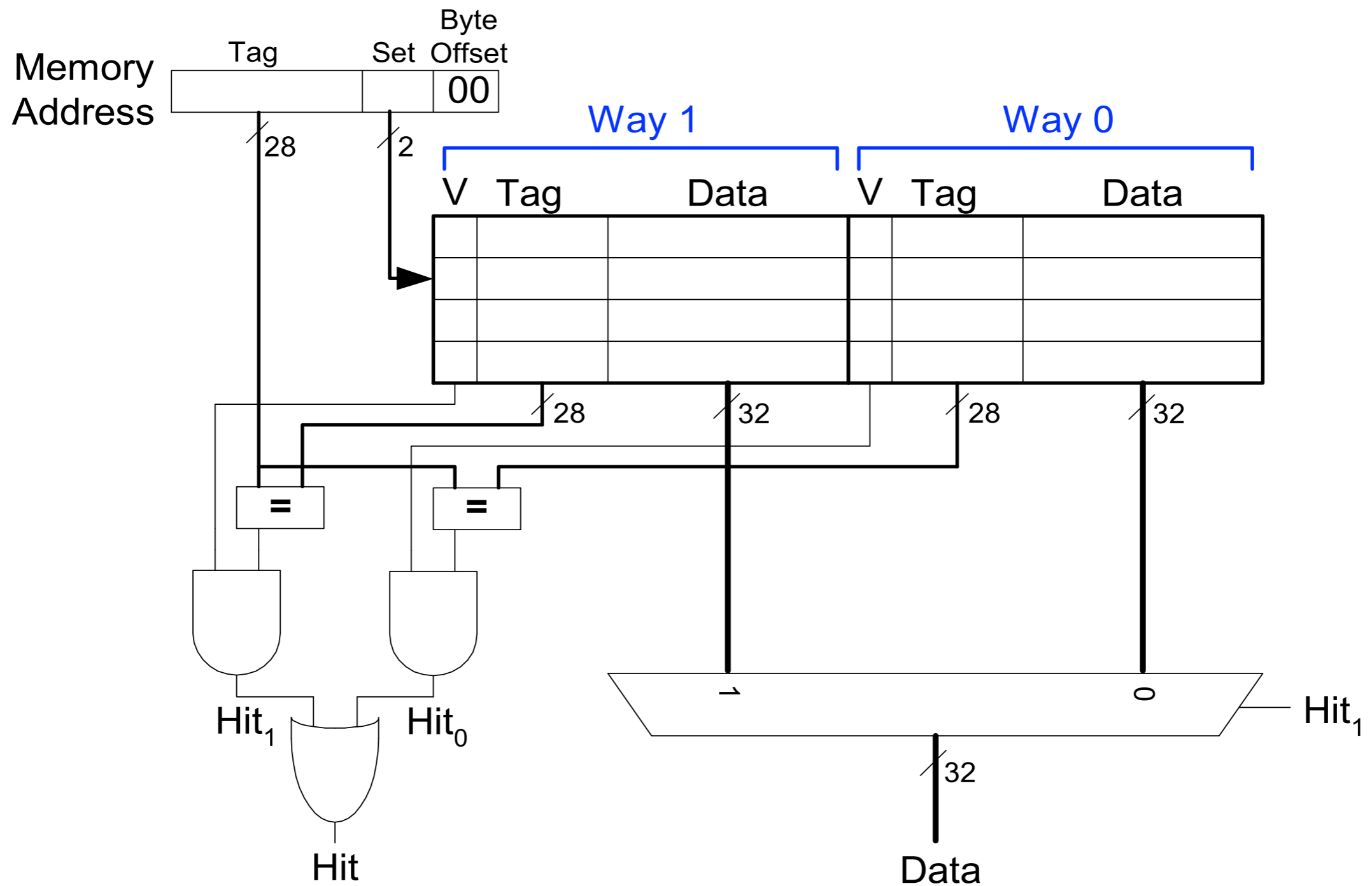


Hash vs. Cache



- Suppose each hash chain is limited to the same, small size (2?)

N-Way Set Associative Cache



Cache Terminology

Capacity (C):

the number of data bytes a cache stores

Block/Line size (b):

bytes of data brought into cache at once

Number of blocks/lines ($B = C/b$):

number of blocks in cache: $B = C/b$

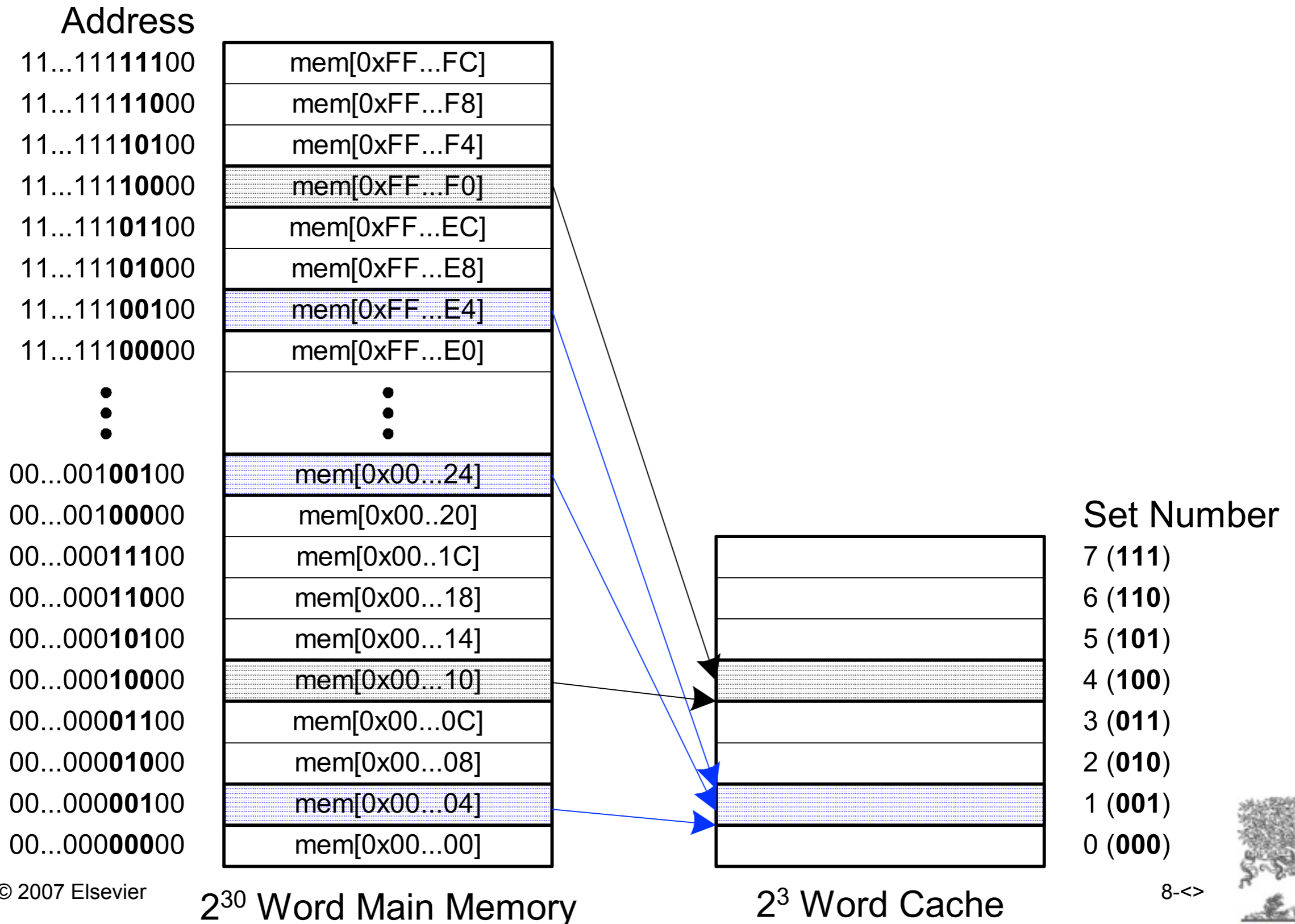
Degree of associativity (N):

number of blocks/lines in a set

Number of sets ($S = B/N$):

each memory address maps to exactly one cache set

Direct Mapped Cache



(Partial) Loop Unrolling

```
for ( i = 0; i < 1000; i++ ) {  
    a[i] = 0;  
}
```

7 instruction loop

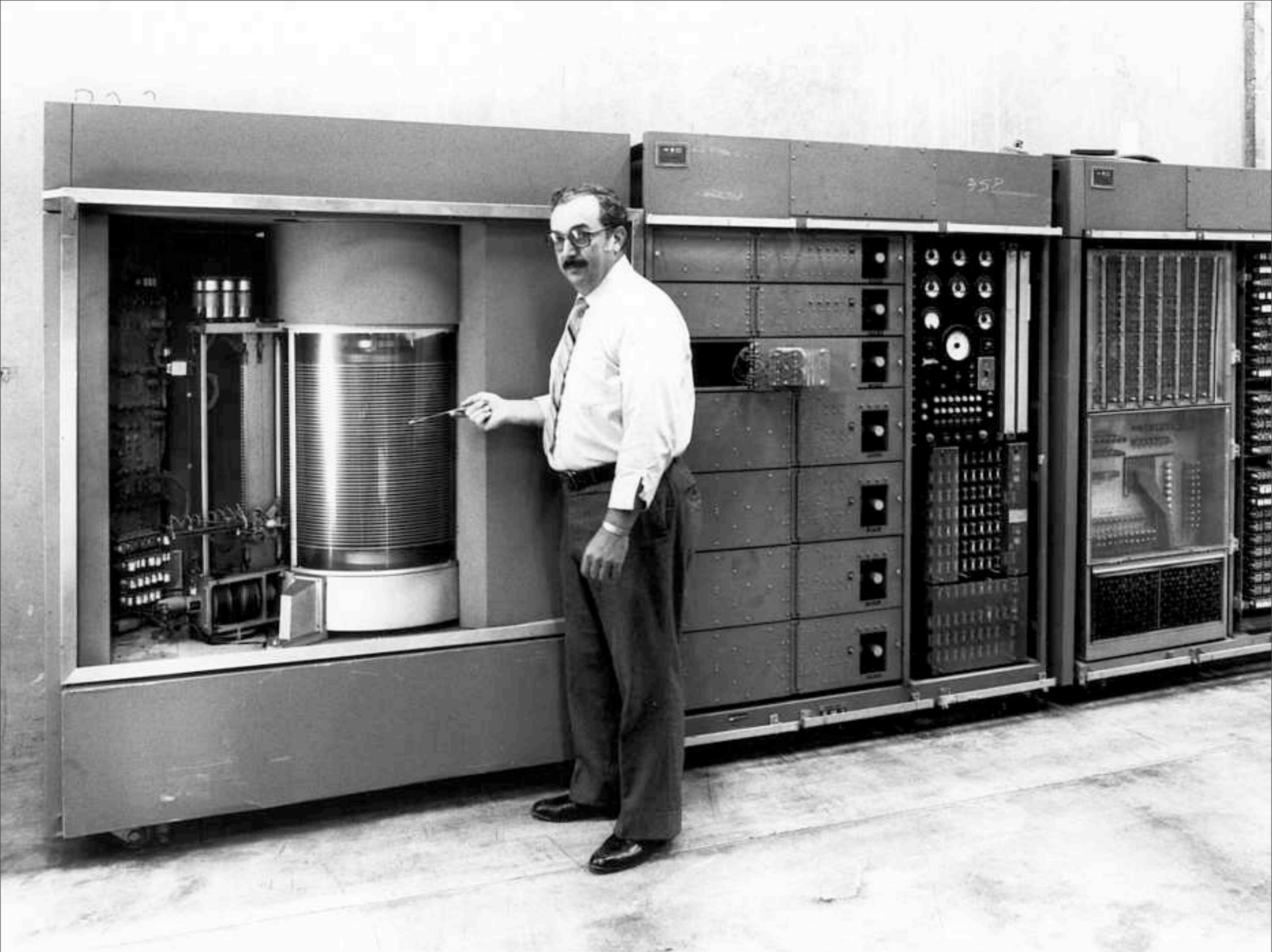
```
    la $t0,a  
#   for(int i=0;i<1000;i++)  
    li $t3,0  
    li $t4,1000  
zeroloop:  
    slt $t5,$t3,$t4  
    beq $t5,$0,zeroloopEnd  
  
#   a[i] = 0;  
    add $t6,$t3,$t0  
    sw $0,0($t6)  
  
    addi $t3,$t3,1  
b zeroloop:  
zeroloopEnd:
```

(Partial) Loop Unrolling

```
for ( i = 0; i < 1000; i = i + 4 ) {  
    a[i] = 0;  
    a[i+1] = 0;  
    a[i+2] = 0;  
    a[i+3] = 0;  
}
```

9 instruction loop

```
    la $t0,a  
#   for(int i=0;i<1000;i=i+2)  
    li $t3,0  
    li $t4,1000  
zeroloop2:  
    slt $t5,$t3,$t4  
    beq $t5,$0,zeroloop2End  
  
#   a[i] = 0;  
    add $t6,$t3,$t0  
    sw $0,0($t6)  
    sw $0,4($t6)  
    sw $0,8($t6)  
    sw $0,12($t6)  
    addi $t3,$t3,4  
b zeroloop2:  
zeroloopEnd2:
```

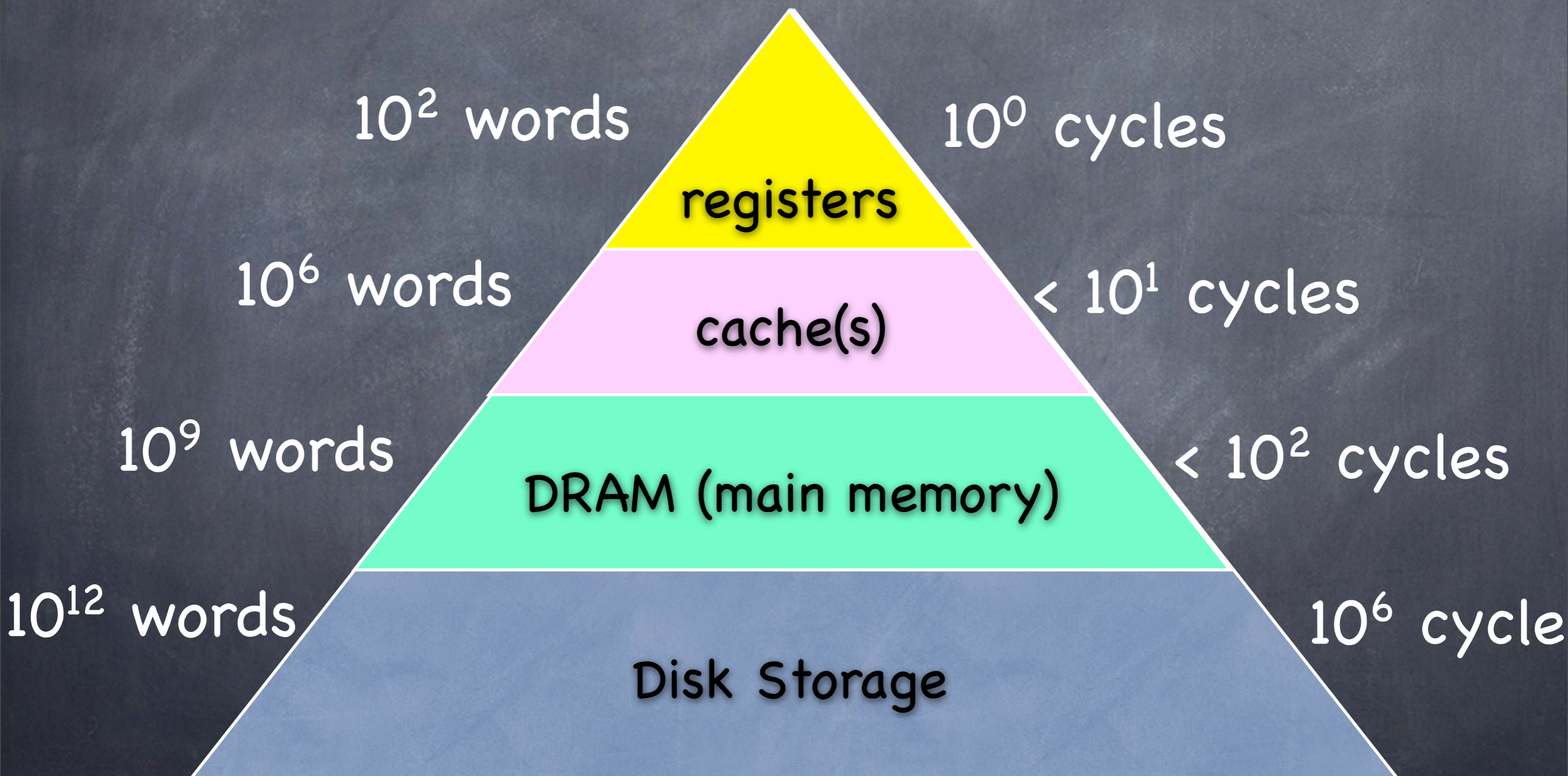




2311 Disk Storage Drives




Virtual Memory?



Cache Miss Penalty

	Cache	DRAM	Disk
	5	25	1000000
0.5	3	13	500001
0.8	1.8	5.8	200001
0.9	1.4	3.4	100001
0.999	1.00	1.02	1001
0.999999	1	1	11
0.9999999	1	1	2


Access time in cycles



Hit Rate



Effective Memory Access Times



$$\text{Effective} = 1 * \text{hit-rate} + \text{access-time} * (1 - \text{hit-rate})$$

Program 2's Virtual Addr Space



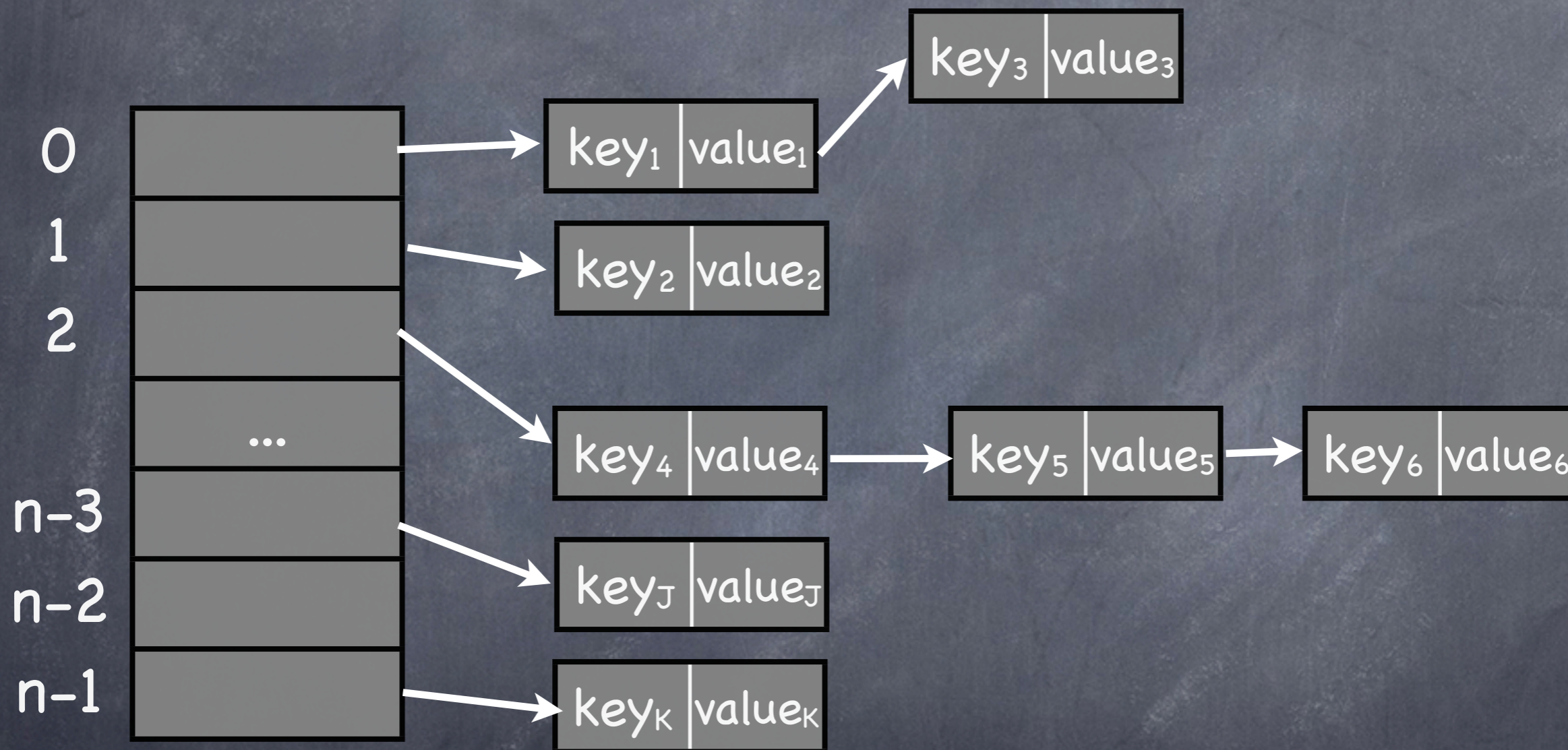
Real/Physical Memory



Program 1's Virtual Addr Space

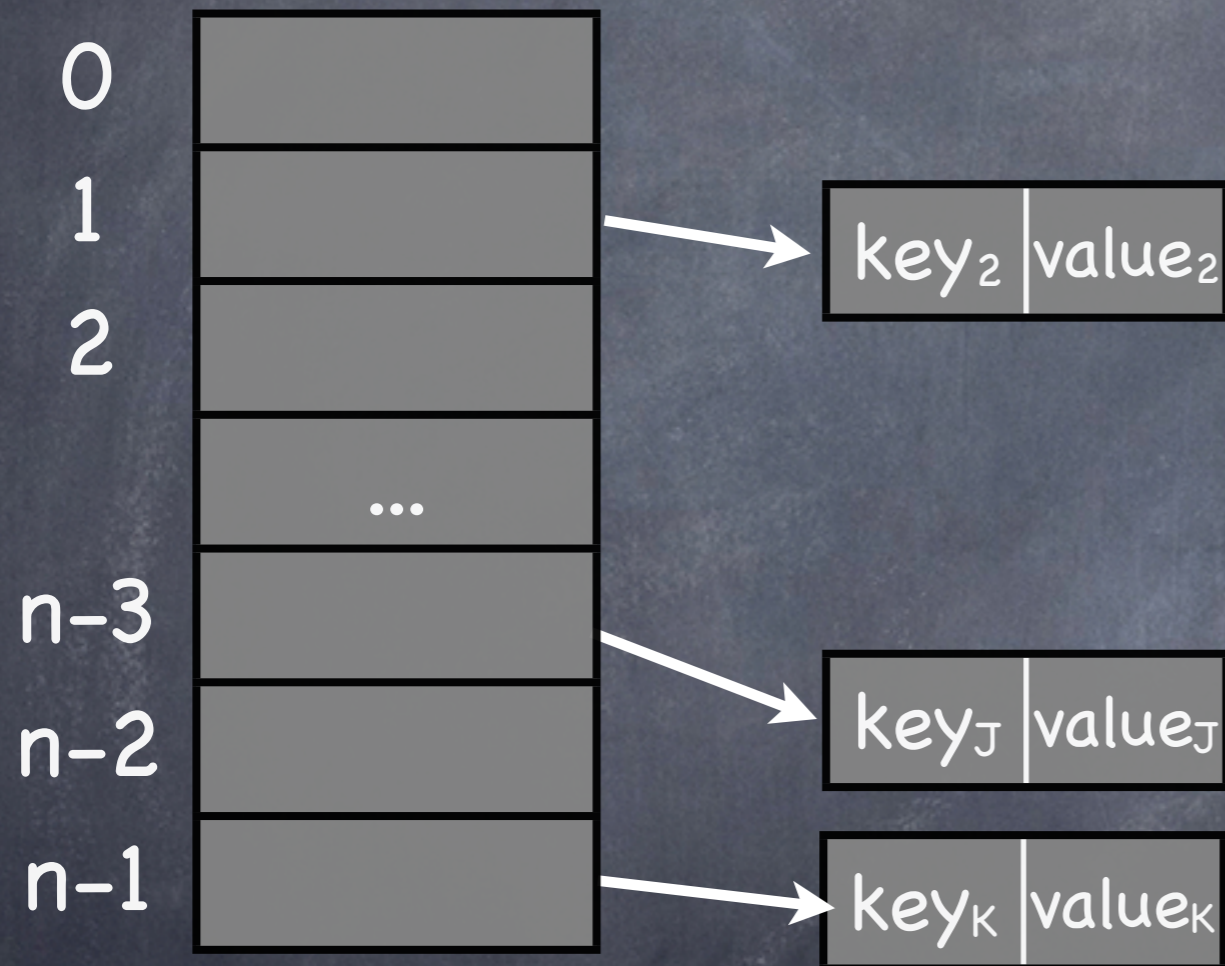


Hash vs. Page Table



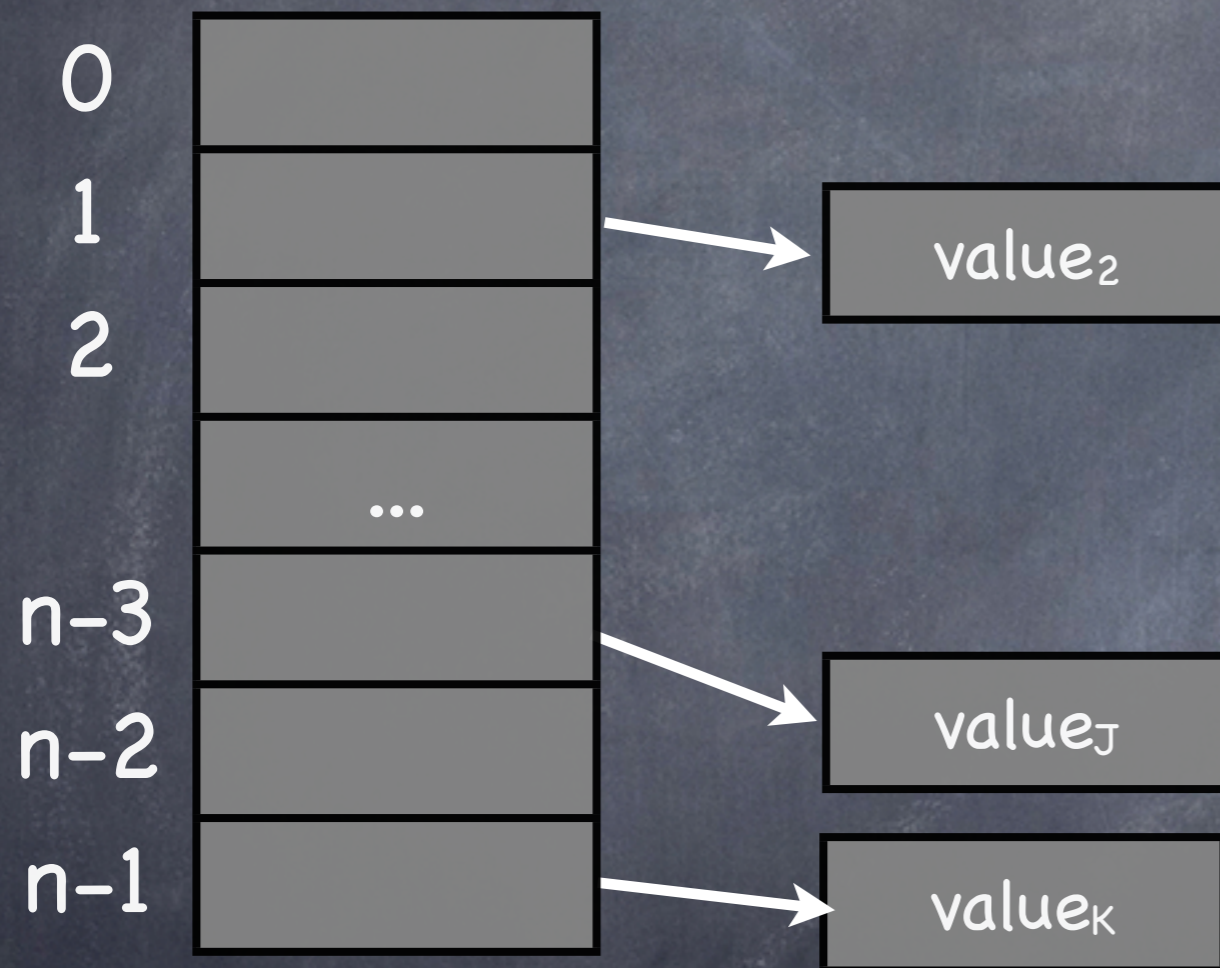
- Can't afford to traverse chains
- Can't afford to discard entries!

Sparse Hash = Page Table



- Let n = number of pages in address space

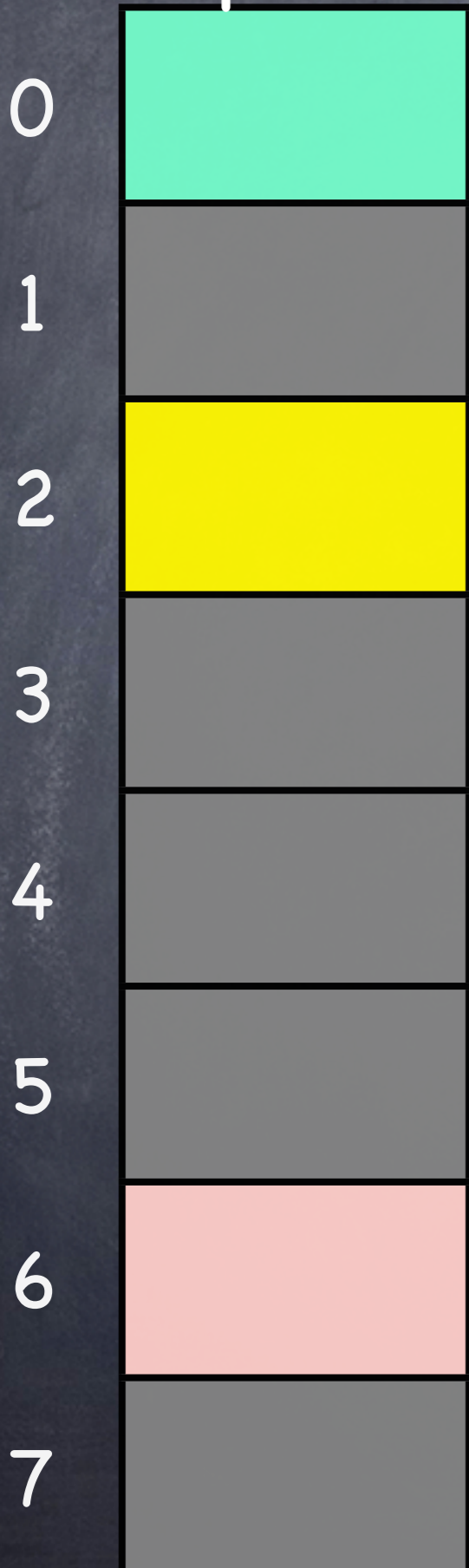
Sparse Hash = Page Table



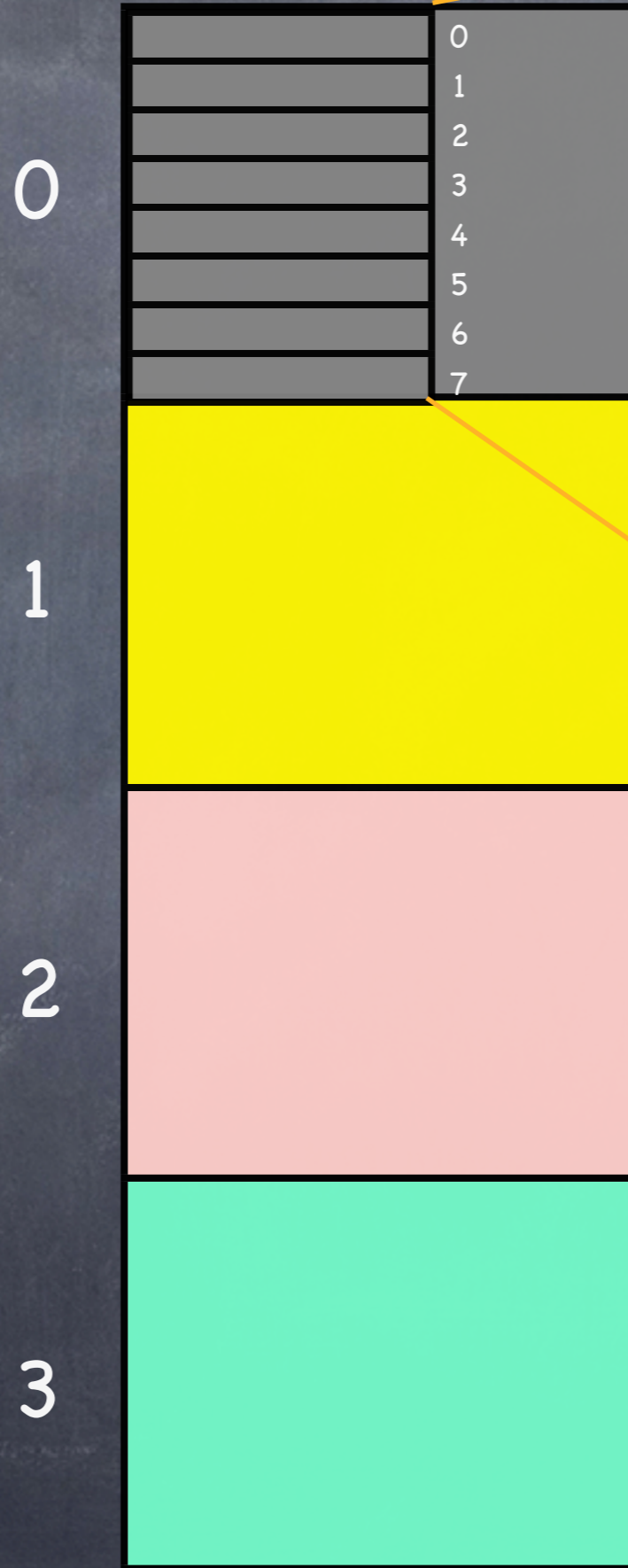
$\text{hash}(x) = x!$

- "Values" in key/value pairs of page table are huge. Can't afford to put them inline.

Virtual Addr Space



Real/Physical Memory



Page Table

3	0
-	1
1	2
-	3
-	4
-	5
2	6
-	7

